

Standards: MCA2 MCA2d

Old Direct Substitution Property If Junction f is a polynomial/rational & (a) is in the domain, then $\lim_{x \to a} f(x) = f(a).$

[FAC] Functions that applied this property are called continuous at (a).



Graph #3 is the only one that is continuous. The basic idea for picking a graph to be continuous is drawing the graph without picking up your pencil."



3 Infinite Discontinuity

vertical asymptote is present at (a).

<u>3 Requirements for a function to be continuous</u> <u>Condition 1</u>: f(a) is defined <u>Condition 2</u>: $\lim_{x \to a} f(x)$ must exist <u>Condition 3</u>: $\lim_{x \to a} f(x) = f(a)$.

[Example1] let's consider a print that is continuous & use the requirements to prove that is continuous.





(X=1 Condition 1: ((1)= d.n.e



(X=4) condition 1: f(4)=4 (Ondition 2: lim (x) = 2 $\frac{\text{Condition 3:}}{2} = f(4)$

[Examples] Where are each of these functions discontinuous. Give a reason why.

(2) $f(x) = \frac{x^2 - x - 2}{x - 2}$ discontinuous at x=2

Xcondition 1: f(2) = d.n.e



One-sided Continuity - The basic idea is the same except we are looking for continuity of one side of the value, vather than both sides.

Definition:
A function
$$f$$
 is continuous from the right
if $\lim_{x \to a^+} f(x) = f(a)$.

· A function is continuous from the left



a) IS X=1 continuous frum the left? NO $\lim_{x \to 1^-} f(x) = f(1)$ $1 \neq d.n.e$

(b) Is X=3 continuous from the left? yes $\lim_{x \to 3^{-}} f(x) = f(3)
 \\
 -2 = -2$

ISX=1 continuous from the right? no $\lim_{x \to 0} f(x) = f(1)$ ×+2+ 1≠ d.n.e

|S X=3 (ontinuous from the right? DD lins f(x)= f(3) 3 ≠ -2

