5.7 Slope Fields with Euler's Method

Standards: MCA3 MCA3a MC11 MC11a

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old Related Rates

A spherical snowball metts in such a way that the instant at which its radius is 20cm, its judius is decreasing at 3 cm/min. At what rate is the volume of the ball changing at thut instant?

given:
$$r = 20 \text{ cm}$$
, $\frac{dr}{dt} = -3 \text{ cm}$, $\frac{dV}{dt}$
20 cm i
Eqtn: $V = 4.7rr^3$
 $\frac{dV}{3} = \frac{4.7rr^3}{3}$
 $\frac{dV}{dt} = \frac{4.7rr^3}{3}$
 $\frac{dV}{dt} = \frac{4.7rr^2}{3} \frac{dr}{dt}$
 $\frac{dV}{dt} = 4.7rr^2 \frac{dr}{dt}$

(New] Slope Fields

Let's consider the following situation : Suppose we are interested in how fast an employee learns at a given task.

rate a person learns = percentage of task not yet learned.

Let y = the percentage learned by time (t weeks).

Equation: $\frac{dy}{dt} = 100 - y \implies$ an example of differential equation.

Differential Equation - is such an equation, that gives information about the rate of change of an UNKNTMENNAFQUERTED by Keenan Xavier Lee, 2013. See my website for more information, lee-apcalculus.weebly.com.

Let's say that work is a 5 day work weekand let's assume 200% of the learning rate holds for the first day. How much does the person need to learn in 1 day? (1 day = 45 of wk) dy = 100-y =100-(20%)= 80% per day We can also visualize differential-equation using SLOPE FIELDS! Let's consider the differential equation: $\frac{dy}{dx} = y \longrightarrow$ Any solution to the differential eqts. has the property that the $\frac{dy}{dx} = y \longrightarrow$ and $\frac{d$ dy = y dx = y
 x
 y
 dy: 7.7

 0
 0
 0

 1
 1
 1

 1
 3
 3

 2
 -3
 -3

 0
 1
 1

 0
 -1
 -1

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Let's find the particular solution to the equation $\frac{dy}{dx} = 2x$ whose graph passes through (1,2)



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